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BGS FACS CHRISTMAS WORKSHOP

'VOM SPEECHING, SLIDES'

An Approach to Structuring for the VDM Specification Language

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REQUIREMENTS

- **Allow a large specification to be split into person sized units, in a natural way.**
- **Allow an individual module, or an incomplete group of modules to be checked.**
- **Limit interference between separate units.**
- **Provide a detailed semantic definition**

SB31

CONSTRAINTS

- It must be possible to compare the semantics of a specification given in the core language with the semantics of a specification given using the structuring constructs.
 - so we use the same basic mathematical machinery.
- The definition of the structuring constructs must preserve the semantics of the core language.
 - so we do not extend the core language.

A CHOICE

- **Use simple unsophisticated mathematics**

SB68



OVERVIEW OF MODULES

- As in STC VDM, the basic specification unit is a **MODULE**.
- A module encapsulates a collection of related types, values, functions and operations.
- Operations within a module may interact by updating values of a shared state.
- A module is similar to an algebraic ADT. It defines a state type which may be used in other modules.
- A module is an object.

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MODULE SYNTAX

Module :: intf : Interface
 body : {Definitions}

Module

- – description of constructs provided by,
- – or used by, the module

Definitions

- – collection of definitions written in
- – the core language, but using constructs
- – introduced by the interface

end

OVERVIEW OF IMPORT-EXPORT CONSTRUCTS

- A module may EXPORT constructs.
- Exported constructs may be imported and used by another module.
- A group of modules may import constructs from each other.
- A construct which is not exported is "hidden". A hidden construct may not be referred to by any other module.

INTERFACE – EXPORT CLAUSE

Interface :: **id** : **Id**
 exp : **ModSig**

ModSig :: **types** : **Name** \xrightarrow{m} [**TypeDef**]
 values : **Name** \xrightarrow{m} [**Type**]
 fns : **Name** \xrightarrow{m} [**FnType**]
 opns : **Name** \xrightarrow{m} [**OpSig**]

Names of constructs with optional syntactic description

FULL CONCRETE SYNTAX FOR EXPORT

Module INTEGER_STACK

exports

types INTEGER_STACK

operations

POP () $\xrightarrow{0}$ INTEGER using INTEGER_STACK

PUSH (INTEGER) using INTEGER_STACK

definitions

end

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CONCRETE SYNTAX WITH IMPLICIT STATE TYPE

Module INTEGER_STACK

exports

operations POP () $\overset{0}{\rightarrow}$ INTEGER
PUSH (INTEGER)

definitions

end

If an operation exported by module M does not specify the state type explicitly, then the state type is M and the type is implicitly imported.

SB38

LIGHTWEIGHT SYNTAX

```
Module INTEGER_STACK
  exports
    operations    POP, PUSH
  definitions
    -----
    POP ()  $\overset{0}{\rightarrow}$  INTEGER
    PUSH (INTEGER)
    -----
end
```

Signatures provided by the definitions need not be repeated in the export clause.

INTERFACE – IMPORT CLAUSE

Interface :: id : Id

...

imp : Id \xrightarrow{m} Mod Sig

exp : ModSig

- Id of module providing imported constructs
- Syntactic description of constructs

IMPLICIT STATE TYPE

Module SYMBOL_TABLE

imports from INTEGER_STACK

**operations POP () ⁰> INTEGER
PUSH (INTEGER)**

end

If an operation imported from a module M does not specify the state tpe explicitly, then the name of the state type is also M and the type is implicitly imported.

LIGHTWEIGHT SYNTAX

Module INTEGER_STACK

Exports

**Operations POP () $\stackrel{0}{\rightarrow}$ INTEGER
 PUSH (INTEGER)**

end

Module SYMBOL_TABLE

imports from INTEGER_STACK

Operations POP, PUSH

end

If a document contains a module which exports a construct and another which imports it, then the signatures need to be repeated.

SB42

NAMES

Name :: prefix : seq1 of Id
local : Id

```
module INTEGER_STACK  
  exports  
    operations POP, PUSH  
-----  
end
```

Names reflect module structure directly – the prefix indicates where the construct is defined.

The full name of POP is INTEGER_STACK.POP

SB43

NAMES OF IMPORTED CONSTRUCTS

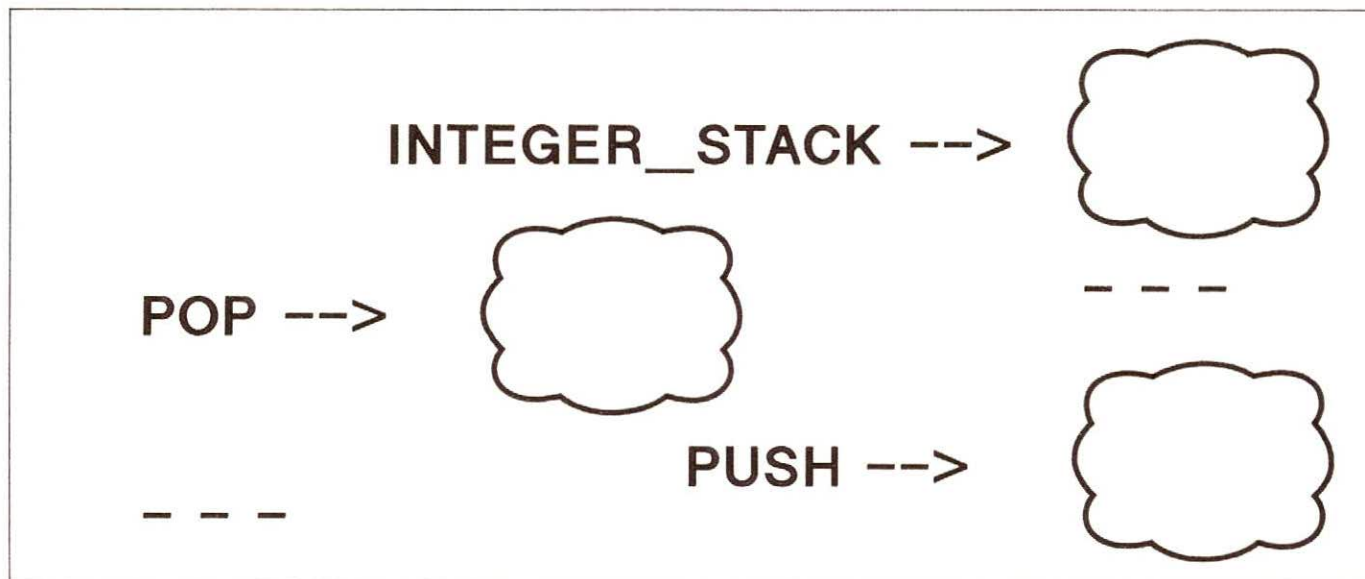
```
Module INTEGER_STACK
  exports
    operations POP, PUSH
---
end
```

```
Module SYMBOL_TABLE
  imports from INTEGER_STACK
    operations POP, PUSH
---
end
```

- The full name of a construct is not changed if it is imported.
- In both modules the full names of POP and PUSH are
INTEGER_STACK.POP
INTEGER_STACK.PUSH

SEMANTICS OF THE CORE LANGUAGE

- The semantics of the core language is given in terms of models.
- A model is a mapping which gives a denotation to a named construct.



SB45

MODELS OF A SPECIFICATION


A model may – or may not – satisfy a specification

definitions


type RED = - - -

type BLUE = - - -

RED ->  - - -

BLUE -> 
- - -

RED ->  - - -

BLUE -> 
- - -

SEMANTICS OF A SPECIFICATION

- The models which satisfy a specification are picked out by a relation

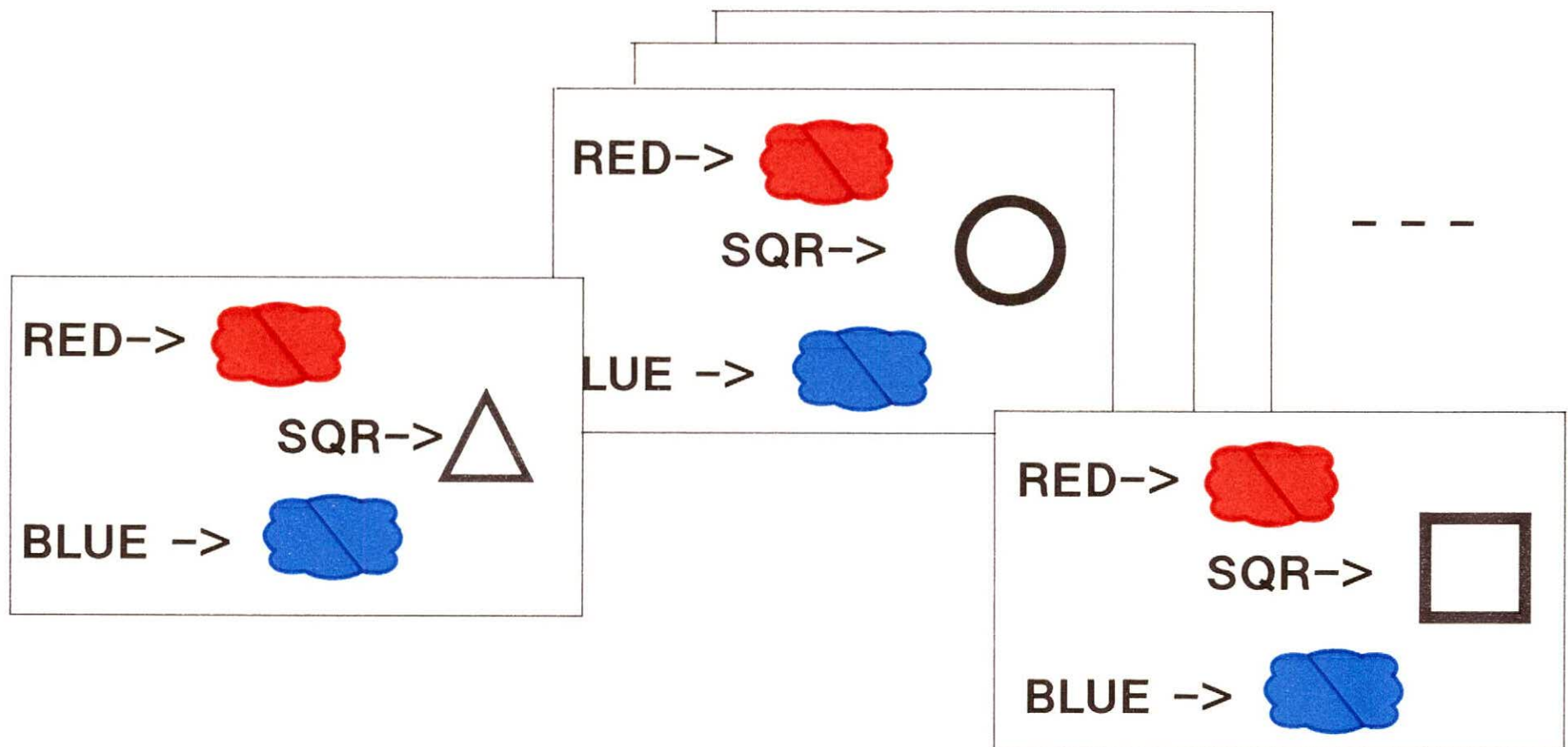
is-a-model-of \subseteq MODELS x Definitions

- The semantics of a specification is defined to be the set of all models which satisfy the specification.

$$[[\text{spec}]] \triangleq \{ M \in \text{MODELS} \mid M \text{ is-a-model-of spec} \}$$

- Defining this relation is a non-trivial task

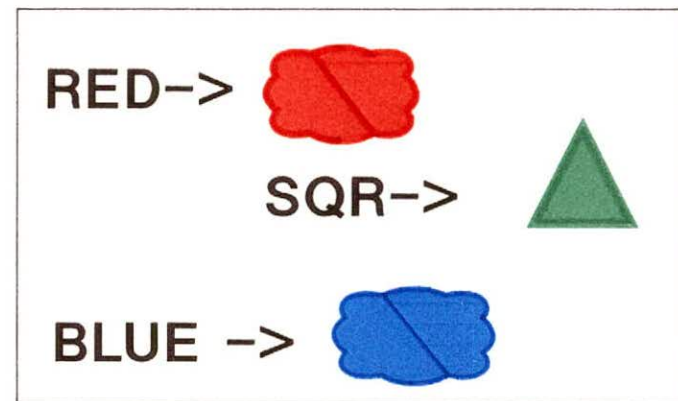
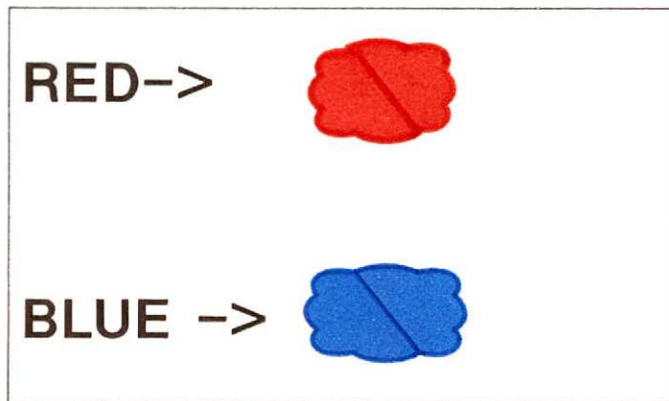
UNDEFINED CONSTRUCTS ARE UNDETERMINED



SB48

MODELS MAY CONTAIN JUNK

- ME $[[\text{spec}]] \wedge n \notin \text{dom}(m) \implies m \cup [n \rightarrow v] \in [[\text{spec}]]$

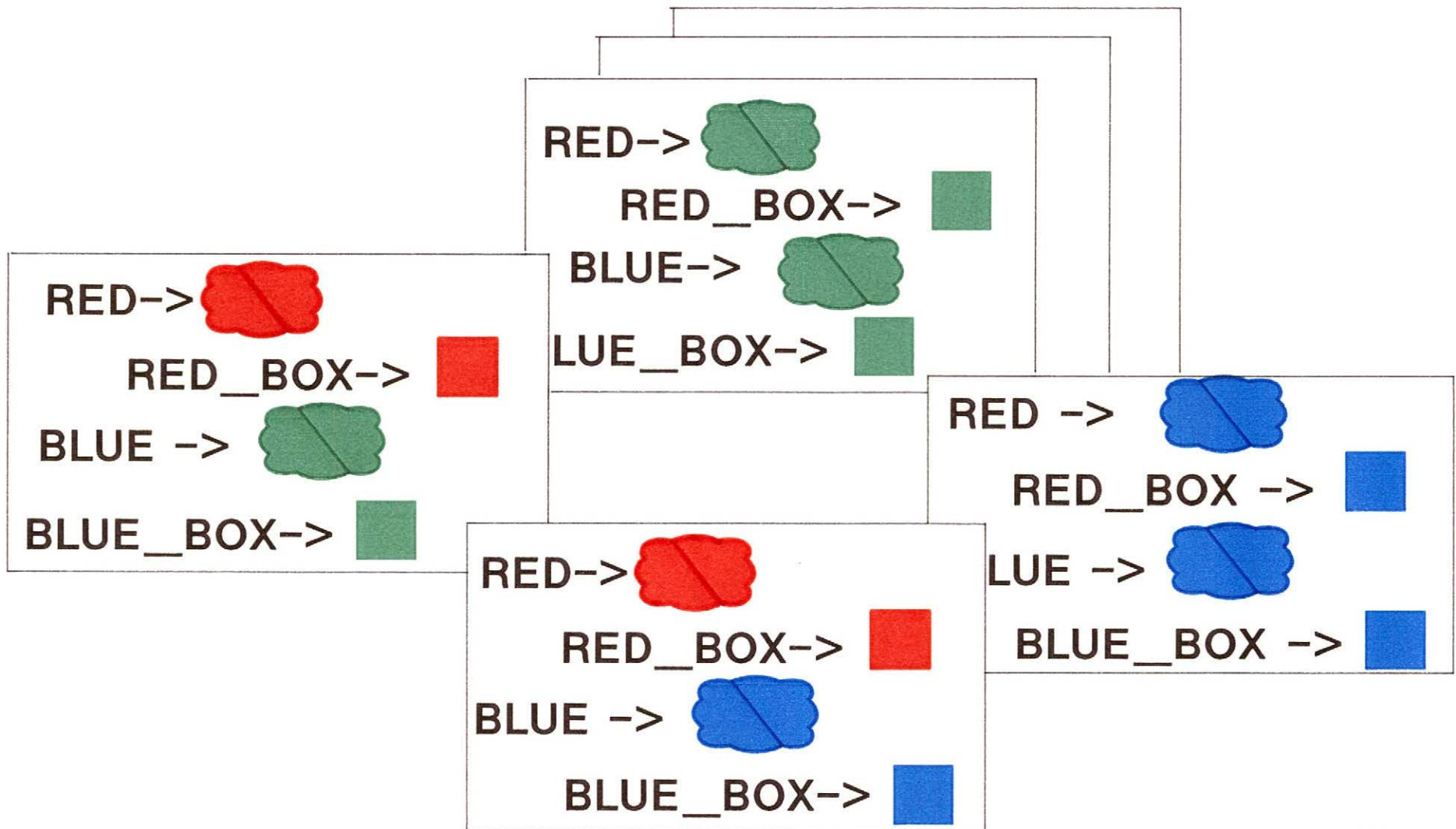


- For any two specifications S, T , if $[[S]]$ is non-empty it contains models which provide denotations for constructs defined or used by T .

```
module COLOURS
    exports
        types RED, BLUE
    definitions
        - - -
    end

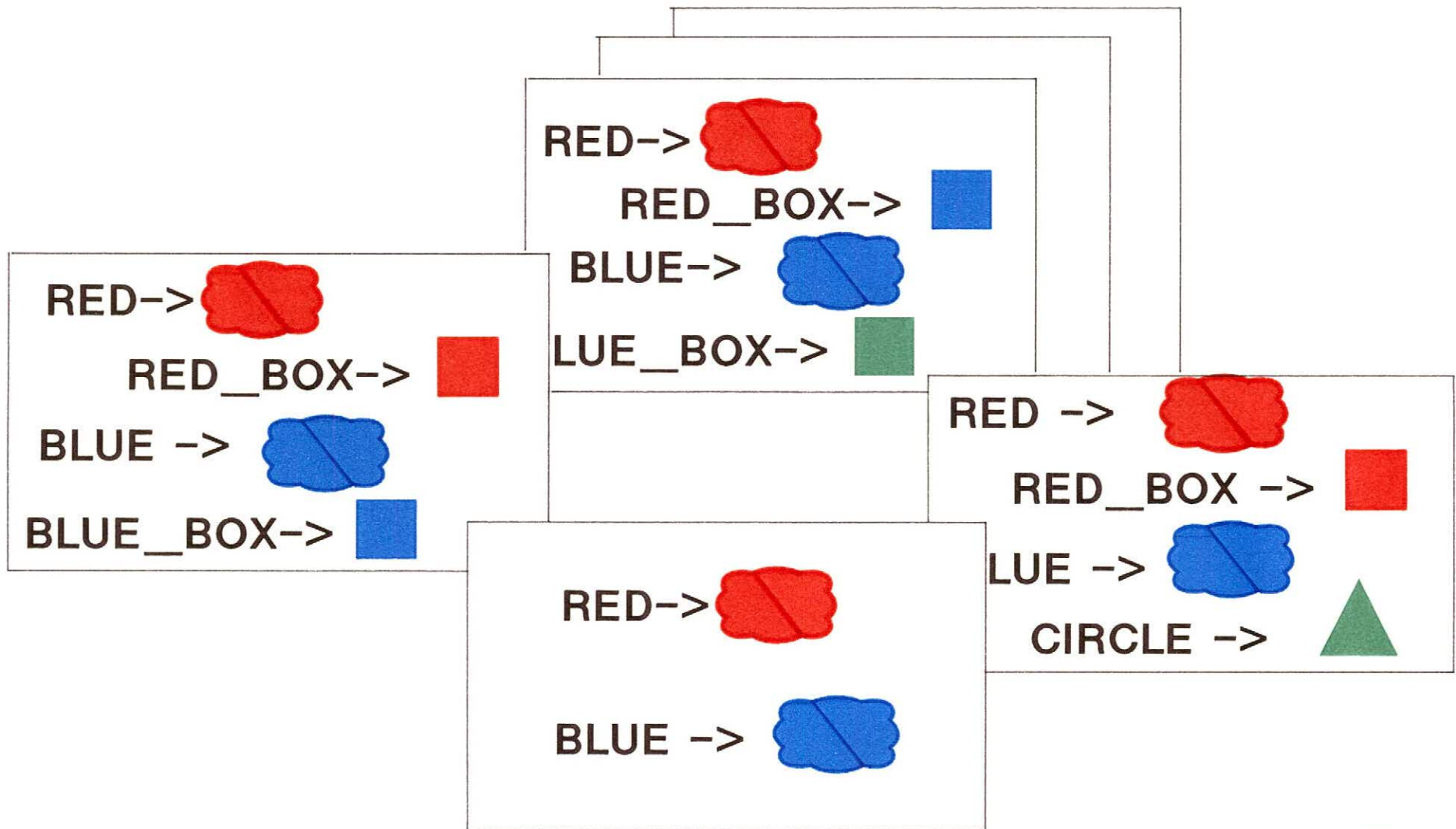
module COLOURED_BOXES
    imports from COLOURS
        types RED, BLUE
    definitions
        RED_BOX = box of RED
        BLUE_BOX = box of BLUE
    end
```


MODELS OF COLOURED_BOXES



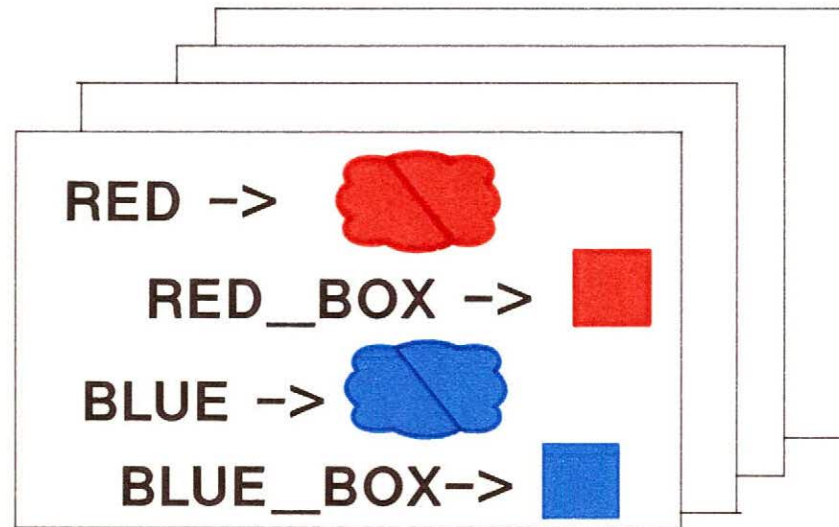
SB51

MODELS OF COLOURS



SB52

MODELS OF THE COMPLETE DOCUMENT



$[[\text{Document}]] \triangle [[\text{COLOURS}]] \wedge [[\text{COLOURED_BOXES}]]$

OVERVIEW OF PARAMETERISATION

- A module may be parameterised by formal parameters – types, values, functions or operations.
- Within the parameterised module, the formal parameters may be used like any other construct.
- A parameterised module may be INSTANTIATED within another module. Formal parameters are replaced by actual parameters.
- Within the instantiating module, the newly instantiated constructs may be used like any other construct.

INTERFACE – PARAMETER CLAUSE

Interface:: **id : Id**
 par : ModSig
 imp : Id \xrightarrow{m} ModSig
 exp : ModSig

Syntactic description of formal parameters

– types, values, functions or operations.

PARAMETERISED MODULE

```
Module SORT
  parameters
    types ITEM
    functions ARE_ORDERED (ITEM,ITEM) --> Boolean
  exports
    functions DO_SORT (seq of ITEM) --> seq of ITEM
end
```

Within a parameterised module, formal parameters may be used like any other constructs.

INSTANTIATION

```
Interface::    id : Id
               part : ModSig
               imp : Id  $\xrightarrow{m}$  ModSig
               inst ; Id  $\xrightarrow{m}$  Instance
               exp : ModSig

Instance::    mod : Id
              view : Id  $\xrightarrow{m}$  Name
              sig : ModSig
```

An instance of a parameterised module may be created
– instantiated – by another module

INSTANTIATION OF SORT

Module SORT

parameters

types ITEM

functions ARE_ORDERED (ITEM,ITEM) --> Boolean

exports

functions DO_SORT (seq of ITEM) --> seq of ITEM

end

Module MAILING_LIST

instantiates

INTEGER_SORT as new SORT

(ITEM --> INTEGER, ARE_ORDERED --> GE)

Functions DO_SORT (seq of INTEGER) --> seq of INTEGER

end

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NAMES OF INSTANTIATED CONSTRUCTS

- Suppose that a parameterised module defines a type T. Then the full name is

P.T

- If a module M creates an instance I of P
module M

instantiates

I as new P (– – –)
type T

The full name of the instantiated construct is

M.I.T

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Module MAILING_LIST

instantiates

 INTEGER_SORT as new SORT
 (ITEM --> INTEGER, ...)

 Functions DO_SORT (seq of INTEGER) --> seq of INTEGER

 ADDRESS_SORT as new SORT

 (ITEM --> ADDRESS, ...)

 Functions DO_SORT (seq of ADDRESS) -->
 seq of ADDRESS

end

- MAILING_LIST.INTEGER_SORT.DO_SORT
- MAILING_LIST.ADDRESS_SORT.DO_SORT

Module COLOURED_BOX

parameters

type COLOUR

exports

type SHAPE

definitions

SHAPE = Box of COLOUR

end

Module BOXES

instantiator

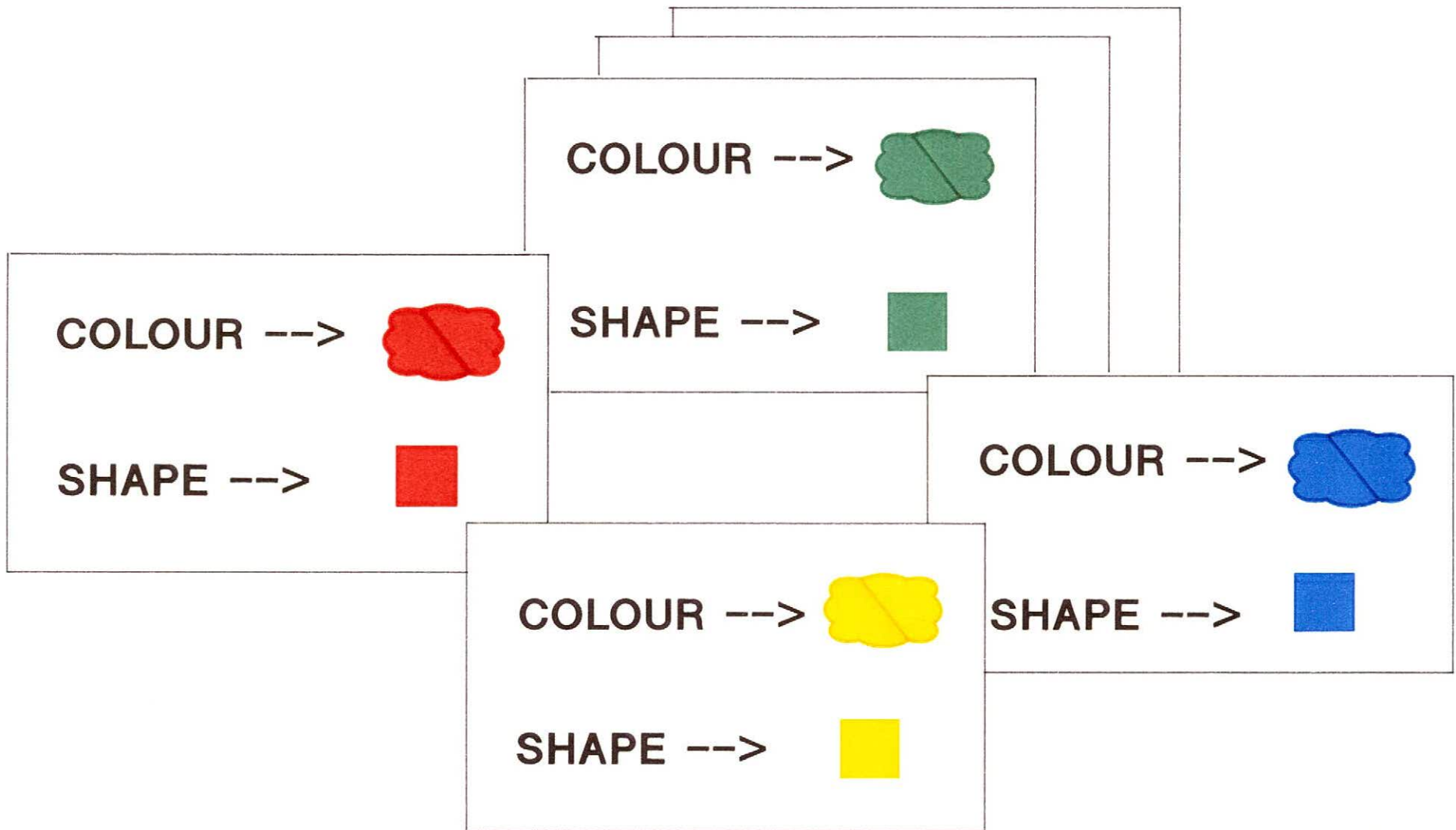
RED_BOX is new COLOURED_BOX
(COLOUR -->RED)

type SHAPE

end

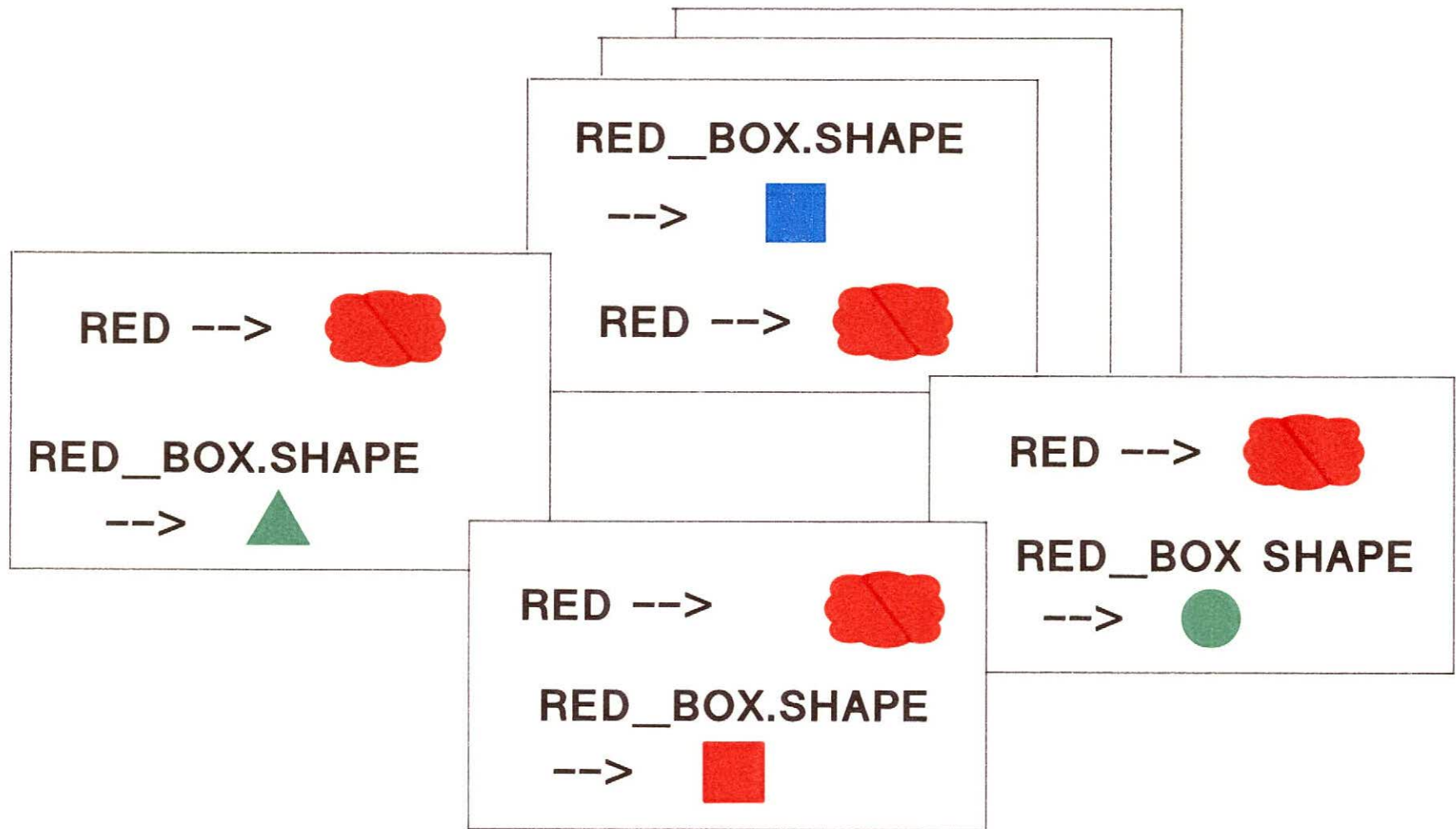
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MODELS OF COLOURED_BOX



SB62

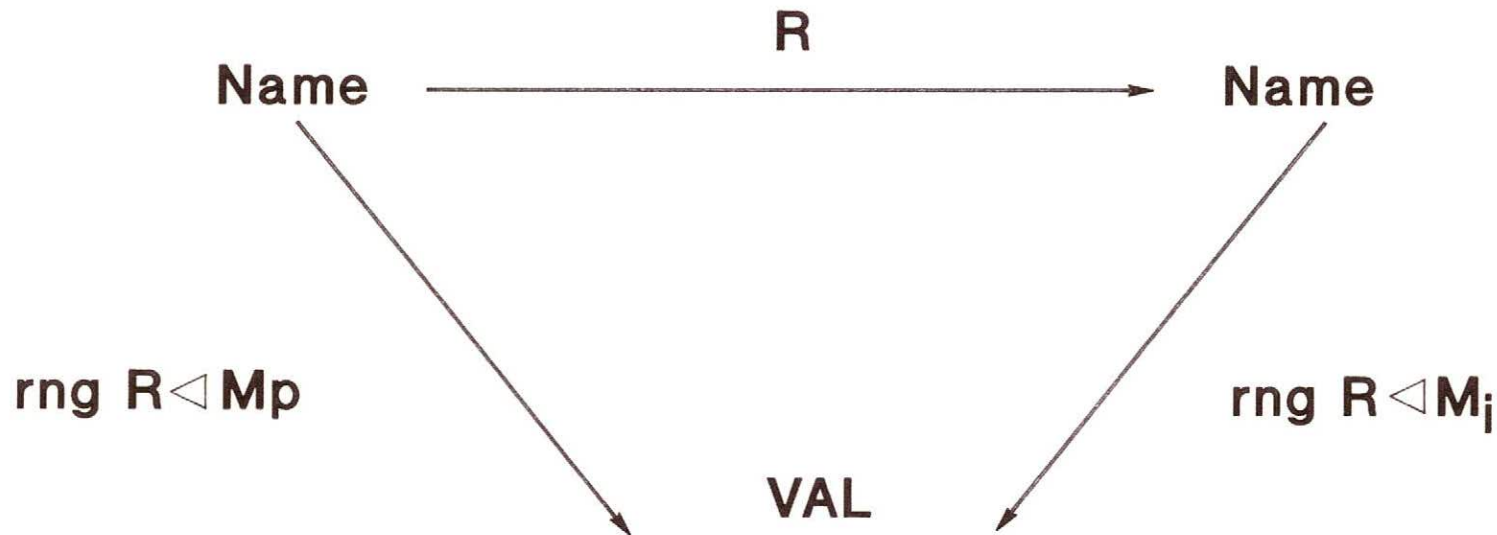
MODELS OF BOXES



SB63

MODELS OF AN INSTANTIATION

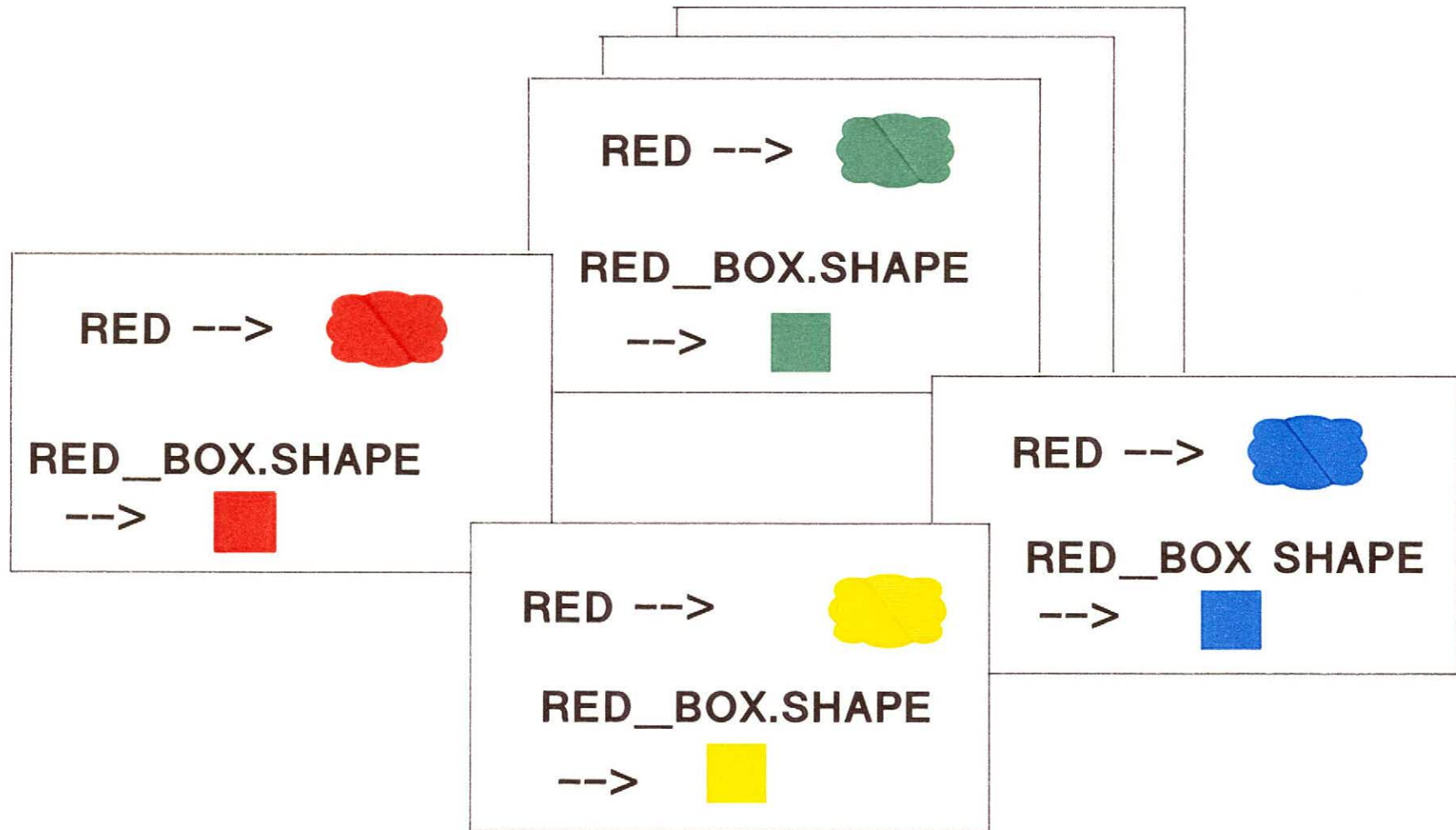
- The models of the parameterised module and the instantiating module can not be compared directly.
- Models of the instantiation.



M_i is a model of the instantiation iff there is a model M_p of the parameterised module such that the diagram commutes.

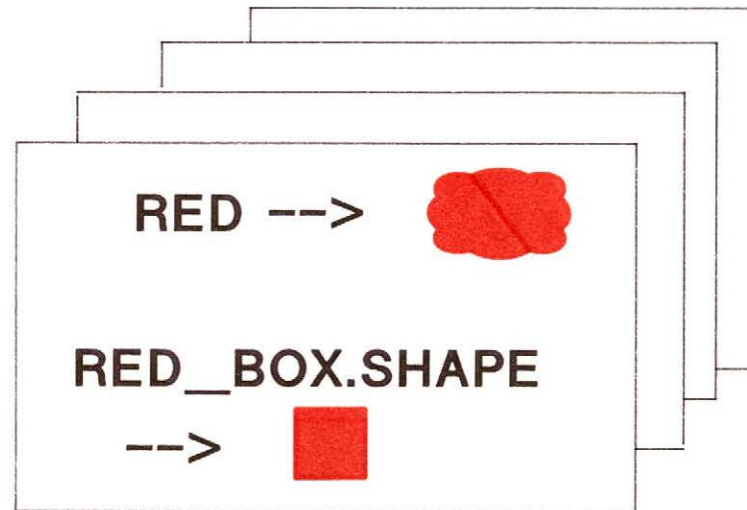
SB64

MODELS OF THE INSTANTIATION



SB65

MODELS OF THE DOCUMENT



$$[[\text{document}]] = [[\text{BOXES}]] \cap [[\text{instantiate}(\text{COLOURED_BOX})]]$$

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SUMMARY

- A specification may be defined as a collection of (parameterized) modules.
- Modules define types – decomposition by types is an established approach.
- The semantics of structuring is defined in terms of the core language.
- The semantics of the core language has not been changed.